

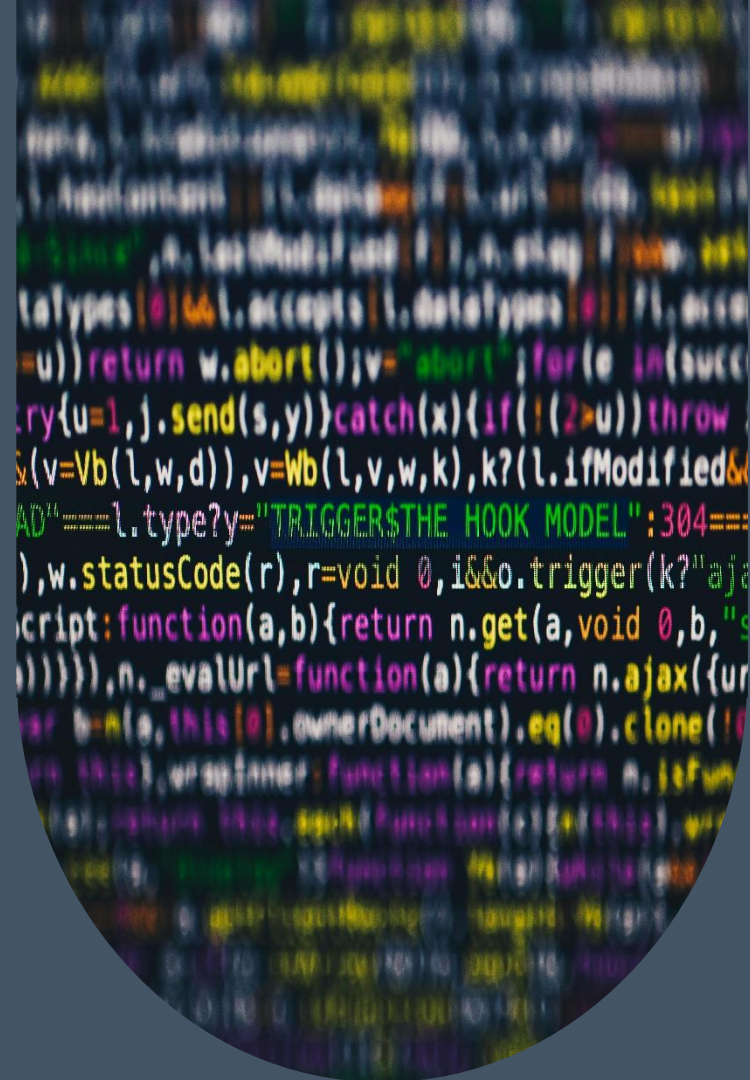
Games ENG II

Chapter 3,

Logic Coverage

Dr. Omer Ali

Adapted from
Introduction to Software Testing (Ammann & Offutt)



Can Graph Coverage identify bugs?

```
#include <iostream> // Function to determine user access
bool hasAccess(bool isAuthenticated, bool isAdmin, bool
isVip) {
    if (isAuthenticated && (isAdmin || isVip))
    {
        return true; }
    return false;
}
```

We need only two test cases to get 100% branch coverage: one that enters the if block (**true** branch) and one that skips it (**false** branch).

Test Case 1 : True branch

isAuthenticated = true, isAdmin = true, isVip = false

Result = hasAccess (true) → Test Passed

Test Case 2 : False branch

isAuthenticated = false, isAdmin = true, isVip = false

Result = hasAccess (false) → Test Passed

Based on that we have 100% branch coverage.

Hidden Bug?

- What if a VIP user is not authenticated but should still get access?
- The business logic requires that **if a user is a VIP, they should have access regardless of their authentication status.**
- The developer made a mistake and included *isAuthenticated* in the condition, preventing this VIP access rule from working.

- Why graph coverage missed it?
- Our branch coverage tests didn't cover the specific logical combination that reveals this bug.
- We need to test the ***individual conditions*** within the if statement more thoroughly.



Testing with Logic Coverage?

- Forcing all logical combinations to identify flaws/bugs
- This is sometimes referred to as Multiple Condition Coverage (MCC)
- MCC requires testing all Boolean conditions within a scope (predicate, more to that later)

Test Case 3 : MCC Coverage

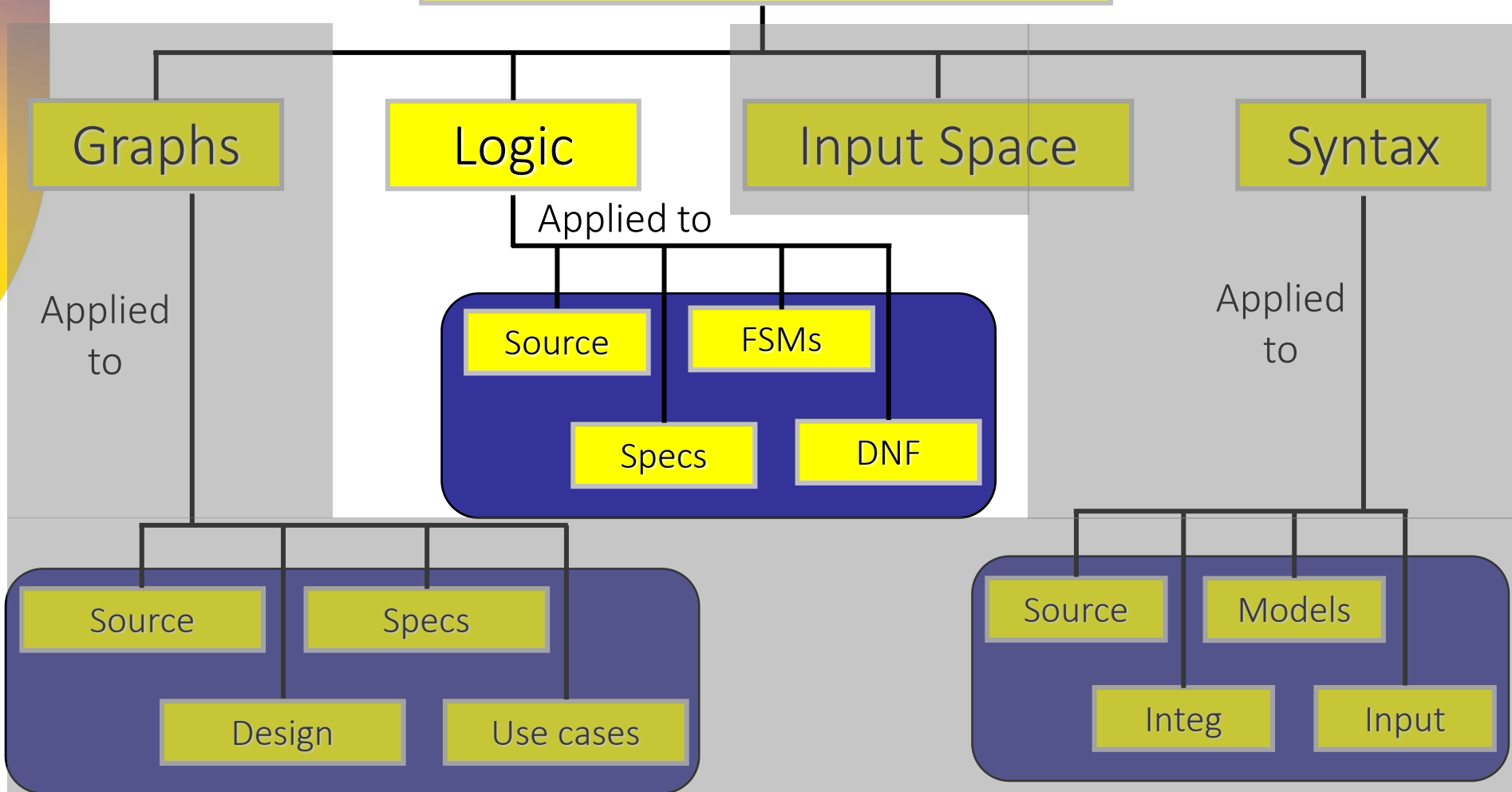
isAuthenticated = false, isAdmin = false, isVip = true

Result = hasAccess (false) → Test Passed

- **The Problem:** The test for a VIP user who is not authenticated *failed*.
- **Expected:** true (if a user is a VIP, they should have access regardless of authentication status).
- **Actual:** false.
- **Conclusion:** The code has a bug! Logic coverage forced us to create a test case that exposed the defect.

Logic Coverage

Four Structures for Modeling Software



Covering Logic Expressions (3.1)

- Logic expressions show up in many situations
- Covering logic expressions is required by the *US Federal Aviation Administration for safety critical software (FAA)*
- Logical expressions can come from many sources
 - Decisions in programs
 - FSMs and statecharts
 - Requirements
- Tests are intended to choose some subset of the total number of truth assignments to the expressions

Logic Predicates and Clauses

- A *predicate* is an expression that evaluates to a **boolean** value
- Predicates can contain
 - **boolean variables**
 - **non-boolean** variables that contain **>, <, ==, >=, <=, !=**
 - **boolean function** calls
- Internal structure is created by logical operators
 - $\neg$: the *negation* operator
 - $\wedge$: the *and* operator
 - $\vee$: the *or* operator
 - $\rightarrow$: the *implication* operator
 - $\oplus$: the *exclusive or* operator
 - $\leftrightarrow$: the *equivalence* operator
- A *clause* is a predicate with no logical operators
 $((a < b) \wedge C) \vee ((a >= b) \wedge p(x))$

Review: Truth Table for Logical Operators

p	q	$p \wedge q$	$p \vee q$	$p \oplus q$	$p \rightarrow q$	$p \leftrightarrow q$
T	T	T	T	F	T	T
T	F	F	T	T	F	F
F	T	F	T	T	T	F
F	F	F	F	F	T	T

Review: the Laws of Logic

1. Commutative Laws

- $p \wedge q \equiv q \wedge p$
- $p \vee q \equiv q \vee p$

2. Associative Laws

- $(p \wedge q) \wedge r \equiv p \wedge (q \wedge r)$
- $(p \vee q) \vee r \equiv p \vee (q \vee r)$

3. Distributive Laws

- $p \wedge (q \vee r) \equiv (p \wedge q) \vee (p \wedge r)$
- $p \vee (q \wedge r) \equiv (p \vee q) \wedge (p \vee r)$

4. Idempotent Laws

- $p \wedge p \equiv p$
- $p \vee p \equiv p$

5. Identity Laws

- $p \wedge F \equiv F$
- $p \vee F \equiv p$
- $p \wedge T \equiv p$
- $p \vee T \equiv T$

6. Involution Law

- $\neg(\neg p) \equiv p$

7. De Morgan's Laws

- $\neg(p \vee q) \equiv (\neg p) \wedge (\neg q)$
(sometimes written p NOR q)
- $\neg(p \wedge q) \equiv (\neg p) \vee (\neg q)$
(sometimes written p NAND q)

8. Complement Laws

- $p \wedge \neg p \equiv F$
- $p \vee \neg p \equiv T$
- $\neg T \equiv F$
- $\neg F \equiv T$

Examples

— $P = (a < b) \vee f(z) \wedge D \wedge (m \geq n * o)$

— P is a predicate

— P has four clauses:

1. $(a < b)$ – relational expression
2. $f(z)$ – boolean-valued function
3. D – boolean variable
4. $(m \geq n * o)$ – relational expression

— Most predicates have few clauses

— It would be nice to quantify that claim !!!

— Sources of predicates

- Decisions in programs
- Guards in finite state machines
- Decisions in UML activity graphs
- Requirements, both formal and informal
- SQL queries (*i.e where conditions*)

From a study of 63 open-source programs, with > 400,000 predicates:

- 88.5% have 1 clause
- 9.5% have 2 clauses
- 1.35% have 3 clauses
- Only 0.65% have 4 or more!

Translating from English

“I am interested in Games ENG II and OOP I”

course = Games2 OR OOP1 = ?

*Humans have
trouble translating
from English to
Logic*

- “If you leave before 6:30 AM, take Braddock to 495, if you leave after 7:00 AM, take Prosperity to 50, then 50 to 495”
- $time < 6:30 \rightarrow path = Braddock \vee time > 7:00 \rightarrow path = Prosperity$
- Hmm ... this is incomplete !
- $time < 6:30 \rightarrow path = Braddock \vee time \geq 6:30 \rightarrow path = Prosperity$

Source Code

```
if ((gear == 5 || gear == 6) && speed >= 100)
    print("highway")
else
    print("some other road");
```

- $P : (g = 5 \vee g = 6) \wedge s \geq 100$

Testing and Covering Predicates

- **We use predicates in testing as follows :**
- Developing a **model of the software** as one or more **predicates**
- Requiring tests to satisfy some combination of clauses
- **Abbreviations:**
- **P** is the set of predicates
- **p** is a single predicate in **P**
- **C** is the set of clauses in **P**
- **C_p** is the set of clauses in predicate **p**
- **c** is a single clause in **C**

Predicate and Clause Coverage

- The first (*and simplest*) two criteria require that each predicate and each clause be evaluated to **both true and false**

Predicate Coverage (PC) : For each p in P , TR contains two requirements: p evaluates to **true**, and p evaluates to **false**.

- When predicates come from conditions on edges, this is equivalent to edge coverage
- **PC** does not evaluate all the clauses, so ...

Clause Coverage (CC) : For each c in C , TR contains two requirements: c evaluates to **true**, and c evaluates to **false**.

Predicate Coverage Example

$$((a < b) \vee D) \wedge (m \geq n * o)$$

predicate coverage

Predicate = true

a = 5, b = 10, D = **true**, m = 1, n = 1, o = 1
= (5 < 10) $\vee$ **true** $\wedge$ (1 $\geq$ 1*1)
= **true** $\vee$ **true** $\wedge$ **TRUE**
= **true**

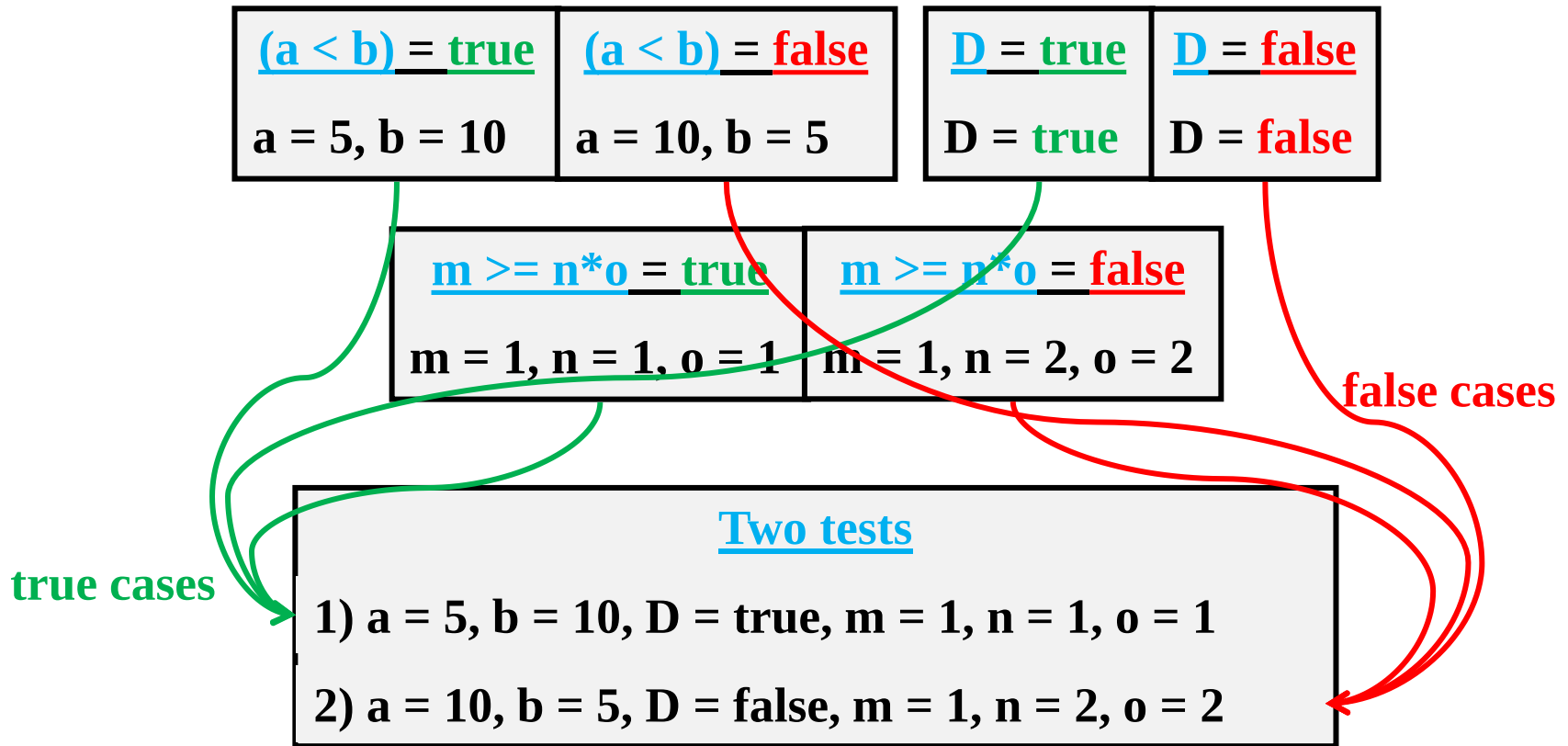
Predicate = false

a = 10, b = 5, D = **false**, m = 1, n = 1, o = 1
= (10 < 5) $\vee$ **false** $\wedge$ (1 $\geq$ 1*1)
= **false** $\vee$ **false** $\wedge$ **TRUE**
= **false**

Clause Coverage Example

$$((a < b) \vee D) \wedge (m \geq n * o)$$

Clause coverage



Problems with PC and CC

	a	b	$p = a \vee b$
1	T	T	T
2	T	F	T
3	F	T	T
4	F	F	F

Examples:

T_{23} : Satisfies CC but not PC, because p is never false

T_{24} : Satisfies PC but not CC, because b is never true

T_{14} : Satisfies both CC and PC coverage

So, neither PC nor CC subsumes the other in all cases.

- PC does not fully exercise all the clauses, especially in the presence of *short circuit evaluation*
- CC does not always ensure PC
- That is, we can satisfy CC without causing the predicate to be both true and false
- This is definitely not what we want !
- The simplest solution is to test all combinations ...

Combinatorial Coverage

- CoC requires every possible combination
- Sometimes called *Multiple Condition Coverage*

Combinatorial Coverage (CoC) : For each p in P , TR has test requirements for the clauses in C_p to evaluate to each possible combination of truth values.

	$a < b$	D	$m \geq n * o$	$P = ((a < b) \vee D) \wedge (m \geq n * o)$
1	T	T	T	T
2	T	T	F	F
3	T	F	T	T
4	T	F	F	F
5	F	T	T	T
6	F	T	F	F
7	F	F	T	F
8	F	F	F	F

Combinatorial Coverage

- This is **simple**, **neat**, **clean**, and **comprehensive** ...
- But quite **expensive**!
- *Requires 2^N tests, where N is the number of clauses*
 - Impractical for predicates with *more than 3 or 4 clauses*
- The literature has lots of suggestions
- The general idea is simple:

Test each clause **independently from the other clauses**

- Getting the details right is hard
- What exactly does “**independently**” mean ?
- The book presents this idea as “*making clauses active*” ...

Active Clauses

- Clause Coverage has a weakness :
 - The values **do not always** make a difference
- Consider the first test for **clause coverage**, which caused each clause to be **true**: $(5 < 10) \vee \text{true} \wedge (1 \geq 1 * 1)$
- Only the last clause **counts** !
- To really test the results of a clause, the clause should be the **determining factor** in the value of the predicate

Determination :

A clause C_i in predicate p , called the **major** clause that **determines** p *iff* the values of the remaining **minor** clauses C_j are such that changing C_i changes the value of p

- This is considered to *make the clause active*

Active Clauses

```

int HonorRollStatus (double CGPA, double termGPA,
int creditsCompleted, Boolean fullTimeStatus)
{
    if ((creditsCompleted > 30) && (CGPA >3.4) &&
(fullTimeStatus == true) && (termGPA >2.5)){
        cout<<"Made it to the Dean's list"<<endl;}
    else if ((creditsCompleted > 30) && (CGPA >3.7)
&& (fullTimeStatus == true) && (termGPA > 2.5)){
        cout<<"The student is on High honor list"<<endl;}
    else if ((creditsCompleted > 30) && (CGPA > 2.5)
&& (fullTimeStatus == true) && (termGPA > 2.5)){
        cout<<"You're on honors list");}
    else{
        cout<<"You're on a 'hit list' somewhere"<<endl;
    }
}

```

Where,

CC = creditsCompleted, FT = fullTimeStatus

TGPA = termGPA

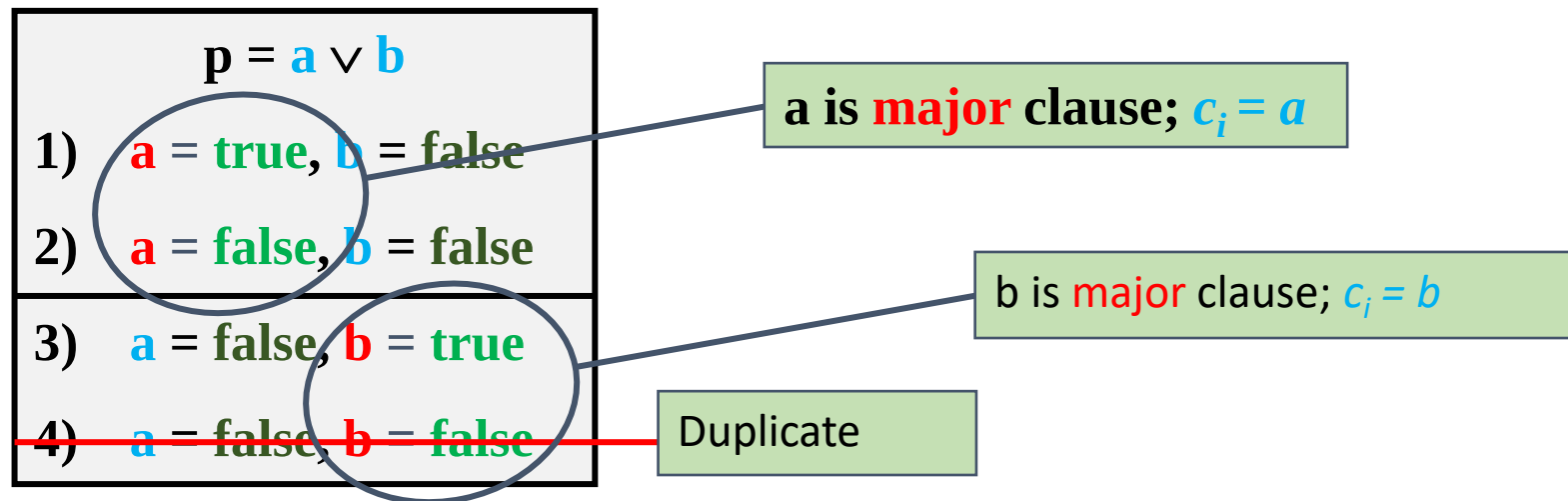
CC	CG PA	FT	TGPA	Honor's List?
29	33	T	2.4	F
31	33	T	2.4	T
31	30	T	2.4	F
31	33	T	2.4	T
31	33	F	2.4	F
31	33	T	2.4	T
31	33	T	1.9	F
31	33	T	2.4	T

Determining Predicates

- Determination, the **conditions** under which a clause **influences** the **outcome** of a **predicate**
- If you **flip** the **clause**, and the predicate changes value, then the clause **determines the predicate**.
- The **major** clause, c_i , is the clause on which we are focusing.
- All of the other clauses $c_j, j \neq i$, are **minor** clauses.
- **Typically**, to satisfy a given criterion, each clause is treated in turn (*One at a time, One by one*) as a **major** clause.
- **From the testing perspective**, we would like to test each clause under circumstances where the clause determines the predicate

Active Clause Coverage

Active Clause Coverage (ACC) : For each p in P and each **major** clause c_i in C_p , choose **minor** clauses c_j , $j \neq i$, so that c_i determines p . **TR** has two requirements for each c_i : c_i evaluates to **true** and c_i evaluates to **false**.



- This is a form of **MCDC** (*Modified Condition/Decision Coverage*), which is required by the FAA for safety critical software
- **Ambiguity** : Do the **minor** clauses have to have the **same values** when the **major** clause is **true** and **false**?

Resolving the Ambiguity

$$p = a \vee (b \wedge c)$$

Major clause : a (or $c_i = a$)

$a = \text{true}, b = \text{false}, c = \text{true}$

$a = \text{false}, b = \text{false}, c = \text{false}$

Is this allowed ?

- Is the **minor** clauses c_j need to have the same values when the major clause c_i is **true** as when c_i is **false** ???
- This question caused **confusion** among testers for years
- Considering this carefully leads to **three** separate criteria :
 1. **Minor** clauses **do not need** to be the same (**GACC**)
 2. **Minor** clauses **do need** to be (**must be**) the same (**RACC**)
 3. **Minor** clauses **force the predicate** to become both **true** and **false** (**CACC**)

General Active Clause Coverage

General Active Clause Coverage (GACC) : For each p in P and each **major** clause c_i in C_p , choose **minor** clauses $c_j, j \neq i$, so that c_i determines p . **TR** has two requirements for each c_i : c_i evaluates to **true** and c_i evaluates to **false**.

Condition: The values chosen for the **minor** clauses c_j **do not** need to be the same when c_i is **true** as when c_i is **false**, that is,

$c_j(c_i = \text{true}) = c_j(c_i = \text{false})$ for all c_j **OR**

$c_j(c_i = \text{true}) \neq c_j(c_i = \text{false})$ for all c_j

- This is **complicated** !
- It is possible to satisfy **GACC** without satisfying predicate coverage (**PC**) . i.e. $p = a \leftrightarrow b$
- We **really want** to cause predicates to be both **true** and **false** !